

Math Packet

Topic 12

Area

Name

Name _____

Area

Topic 12 Standards

6.G.A.1, 6.G.A.3, 6.G.A.4

See the Student Edition lessons for complete standards.

Dear Family,

Your child is learning about finding the area of squares, rectangles, parallelograms, and triangles. You can help him or her become more comfortable finding areas by doing the following activity.

Scavenger Hunt

You will need a ruler, yardstick, or measuring tape.
Find each of the following items around your home.

1. Something square that is an area of less than 20 square inches

Item: _____

A = _____

2. Something rectangular that has an area of more than 75 square inches

Item: _____

A = _____

3. Something square that has an area of more than 30 square inches

Item: _____

A = _____

4. Find the area of a room in your house.

A = _____

Observe Your Child

Focus on Math Practice 6:

Attend to precision.

Help your child become proficient with Math Practice 6. As your child records the measurements, be sure he or she records both an accurate measurement and an appropriate unit. Ask your child to explain to you why recording units is important. Repeat the measurement using different units and discuss the differences in the result.

Nombre _____

Perímetro y área

Estimada familia:

Su niño(a) está aprendiendo a hallar el perímetro y el área de cuadrados, rectángulos, paralelogramos y triángulos. Todo esto requiere que su niño(a) aplique fórmulas. Usted puede ayudarlo(a) a familiarizarse con estas fórmulas realizando esta actividad.

La búsqueda del tesoro

Necesitará una regla, una regla de 1 yarda o una cinta de medir.

Busque cada uno de los siguientes objetos en su casa o sus alrededores.

1. Algo cuadrado que tenga un perímetro de menos de 20 pulgadas cuadradas

Objeto: _____

$P =$ _____

2. Algo rectangular con un área de más de 75 pulgadas cuadradas

Objeto: _____

$A =$ _____

3. Algo cuadrado que tenga un área de más de 30 pulgadas cuadradas

Objeto: _____

$A =$ _____

4. Algo rectangular que tenga un perímetro de menos de 20 pulgadas

Objeto: _____

$P =$ _____

5. Algo cuadrado que tenga un área de menos de 36 pulgadas cuadradas

Objeto: _____

$A =$ _____

6. Algo rectangular que tenga un perímetro mayor que 15 pulgadas

Objeto: _____

$P =$ _____

¡Bono!

7. Halle el perímetro y el área de un cuarto de su casa.

$P =$ _____

$A =$ _____

Name _____

area

area

The amount of surface
that a figure covers.

Lesson 12-1



trapezoid

trapezoid

A quadrilateral that has
only one pair of opposite
sides that are parallel.

Fold here

Lesson 12-4

kite

kite

A quadrilateral with 2 pairs
of adjacent sides that are
equal in length.

Lesson 12-4

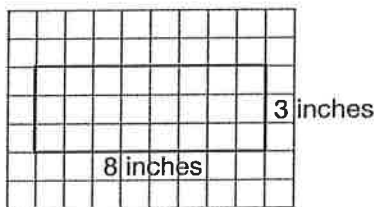
Name _____

Area of Rectangles

Find the area of a rectangle that is 8 inches long and 3 inches wide.

Use Counting

Draw the rectangle on grid paper. Let each square represent 1 square inch.



Count the squares inside the rectangle. There are 24 squares, so the area is 24 sq in.

Use a Formula

Use the formula for area. To find area, multiply length times width.

$$A = \ell \times w \quad \ell = \text{length}, w = \text{width}$$

$$A = 8 \times 3 \quad \ell = 8, w = 3$$

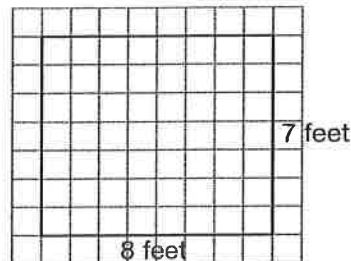
$$A = 24$$

The area of the rectangle is 24 in².

A garden measures 8 ft by 7 ft. What is the area of the garden?

Use Counting

Draw the figure on grid paper. Let each square represent 1 square foot.



Count the squares inside the garden. There are 56 squares, so the area is 56 sq ft.

Use a Formula

Find the area of the rectangular garden by multiplying length times width.

Garden:

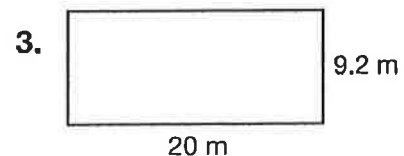
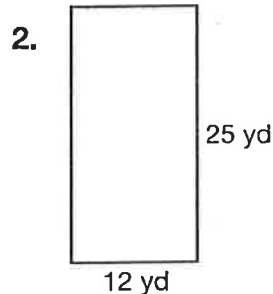
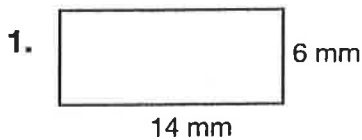
$$A = \ell \times w$$

$$A = 8 \times 7$$

$$A = 56 \text{ sq ft}$$

The area of the garden is 56 ft².

Find the area of each figure.

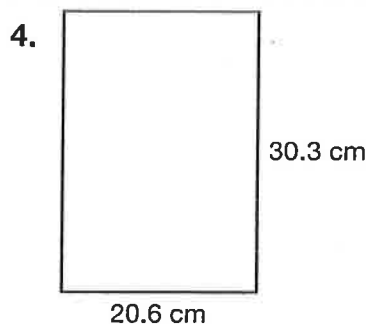
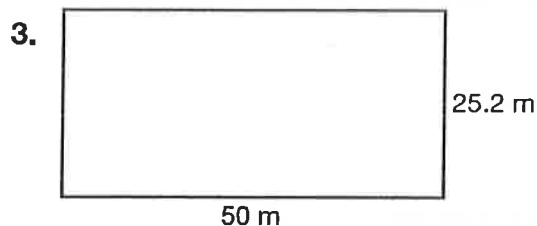
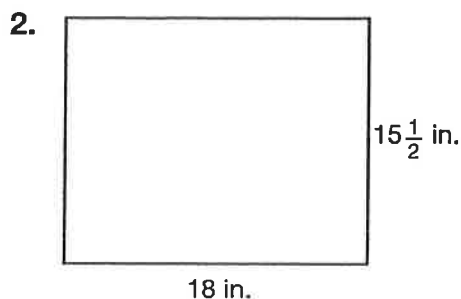
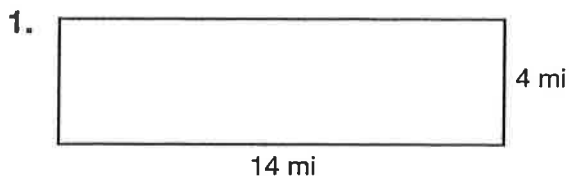


4. Suppose a rectangular garden measures $4\frac{1}{2}$ feet by 10 feet. What is the area of the garden? _____

Name _____

Area of Rectangles

Find the area of each figure.



For 5 and 6, draw and label the figures described using grid paper. Then calculate the area of each figure.

5. A rectangle that is 13 units by 9 units

6. Carlos is laminating a kitchen counter that has dimensions of 12 feet by 3 feet. What is the area of the kitchen counter that Carlos will laminate?

7. What is the area of a square that is 30 centimeters on one side?

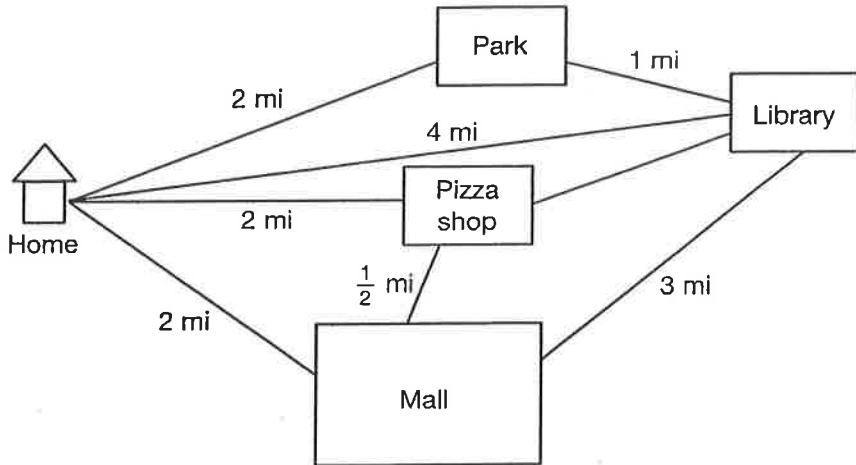
- A 60 cm^2 B 120 cm^2 C 300 cm^2 D 900 cm^2

8. **Writing to Explain** If you know the area of a rectangle, can you determine its length and width? Explain.

Making Plans

Use the information in the diagram and the questions to plan a trip to one or more of the places shown. You can only travel on the paths shown. Remember to plan to spend some time at each place you visit.

Decision Making



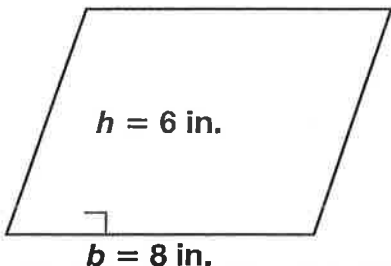
- Plan an outing that will take about 2 hours. You will be traveling by bike at a rate of 6 miles per hour. You must start and finish your trip at home. You must visit at least one location shown on the map. Where will you go? How much time will you spend riding your bike? How much time will you spend at each location? Exactly how long will your trip take?

- Plan an outing that will take about 4 hours. This time, your little sister needs to tag along, so you can only bike 4 miles per hour. You must start and finish your trip at home. You must visit at least two locations shown on the map. Where will you go? How much time will you and your sister spend riding your bikes? How much time will you spend at each location? Exactly how long will your trip take?

Name _____

Area of Parallelograms and Rhombuses

Find the area of this parallelogram.



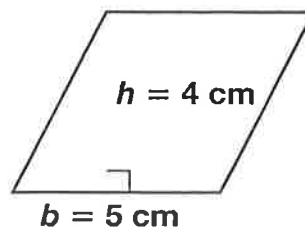
Use the formula $A = bh$.

$$A = 8 \times 6$$

$$A = 48 \text{ in}^2$$

The area of the parallelogram is 48 sq in.

Find the area of this rhombus.



Use the formula $A = bh$.

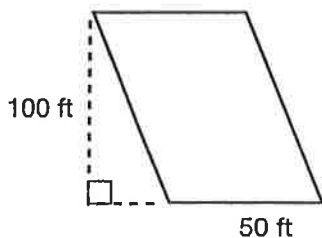
$$A = 5 \times 4$$

$$A = 20 \text{ cm}^2$$

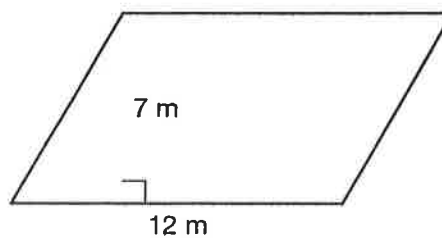
The area of the rhombus is 20 cm².

Find the area of each parallelogram or rhombus.

1.



2.

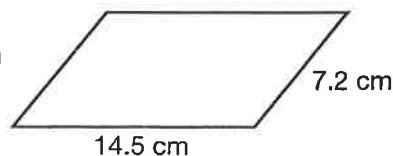


3. Rhombus: $b = 6 \text{ ft}$, $h = 4 \text{ ft}$

4. Parallelogram: $b = 18 \text{ m}$, $h = 13.5 \text{ m}$

5. Parallelogram: $b = 20 \text{ in.}$, $h = 9\frac{1}{2} \text{ in.}$

6. **Writing to Explain** Tony says he does not have enough information to find the area of this parallelogram. Is he correct? Explain.

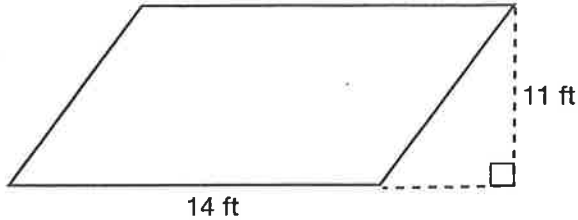


Name _____

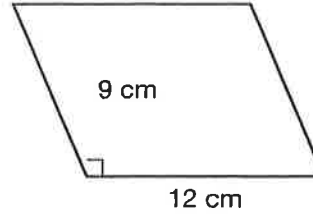
Area of Parallelograms and Rhombuses

Find the area of each parallelogram or rhombus.

1.



2.



3. Rhombus
 $b = 30$ m
 $h = 15.5$ m

4. Parallelogram
 $b = 18$ in.
 $h = 2\frac{1}{2}$ in.

5. Parallelogram
 $b = 20$ ft
 $h = 3$ yd

6. **Writing to Explain** The area of a parallelogram is 42 square inches. The parallelogram's base is 6 inches. Find the height of the parallelogram. Explain how you do it.

7. **Number Sense** A parallelogram has a base of 4 m and a height of 3 m. Find the area of the parallelogram in square centimeters.

8. **Estimation** Which is the best estimate of the area of a parallelogram that has a base of 11.42 cm and a height of 8.33 cm?

- A 200 cm² B 160 cm² C 100 cm² D 50 cm²

9. **Reasoning** The area of a figure is 36 cm². Give 3 possible shapes of the figure. Where possible give 3 possible sets of dimensions for each possible shape.

Name _____

Fantastic Formulas

Choose a formula from the chart to solve the problems below. There may be more than one formula that would work for each problem. Show your work.

Data

Formula File

$$\text{inches} \times 2.54 = \text{centimeters}$$

$$\text{miles} \times 1.61 = \text{kilometers}$$

$$\text{kilometers} \times 0.62 = \text{miles}$$

$$\text{ounces} \times 28.35 = \text{grams}$$

$$\text{centimeters} \times 0.39 = \text{inches}$$

$$\text{pounds} \times 0.45 = \text{kilograms}$$

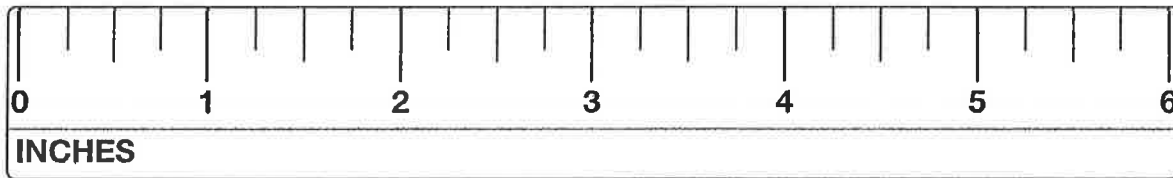
$$\text{meters} \times 1.09 = \text{yards}$$

$$\text{grams} \times 0.04 = \text{ounces}$$

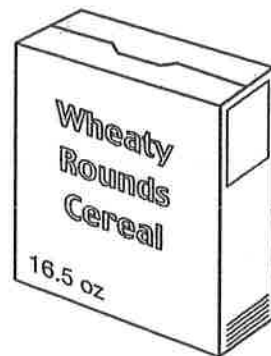
$$\text{yards} \times 0.91 = \text{meters}$$

$$\text{kilograms} \times 2.2 = \text{pounds}$$

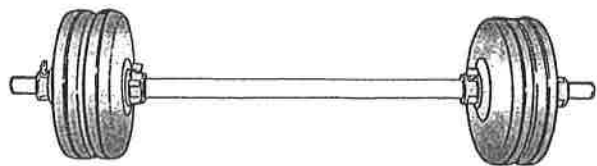
1. How many centimeters long is this pencil?




2. How many grams of cereal does this box measure?



3. How many kilograms does this dumbbell measure?

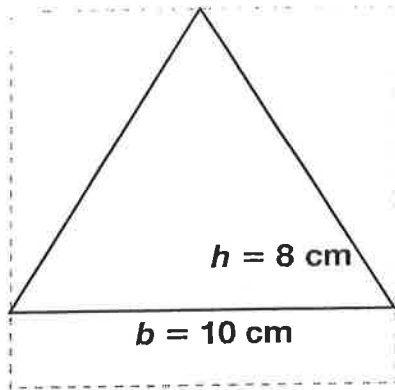


Each  = 50 lb.

Name _____

Area of Triangles

Find the area of this triangle.

Use the formula $A = \frac{1}{2}bh$.

$$A = \frac{1}{2} \times 10 \times 8$$

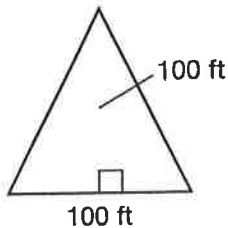
$$A = 5 \times 8$$

$$A = 40 \text{ cm}^2$$

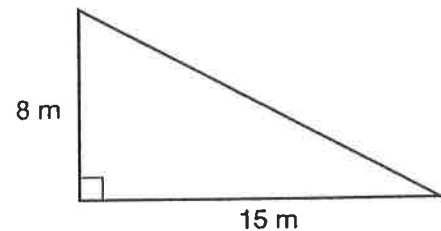
The area of the triangle is 40 cm^2 .

Find the area of each triangle.

1.



2.

3. Triangle: $b = 6 \text{ ft}$, $h = 9 \text{ ft}$ 4. Triangle: $b = 18 \text{ m}$, $h = 13 \text{ m}$ 5. Triangle: $b = 20 \text{ in.}$, $h = 9\frac{1}{2} \text{ in.}$

6. **Writing to Explain** Rebekah needs to find the area of a right triangle. She knows all the side lengths of the right triangle, but she says that she also needs to know the height. Is she correct? Explain.

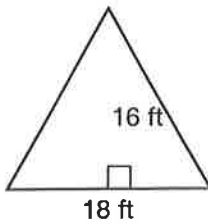


Name _____

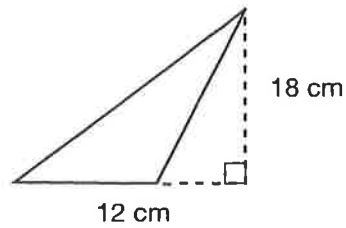
Area of Triangles

Find the area of each triangle.

1.



2.



3. Triangle

$$b = 30 \text{ m}$$
$$h = 15.6 \text{ m}$$

4. Triangle

$$b = 18 \text{ in.}$$
$$h = 6\frac{1}{2} \text{ in.}$$

5. Triangle

$$b = 20 \text{ ft}$$
$$h = 3 \text{ yd}$$

6. **Writing to Explain** The area of a triangle is 42 square inches. The triangle's base is 6 inches. Find the height of the triangle. Explain how you do it.

7. **Number Sense** A triangle has a base of 2 m and a height of 4 m. Find the area of the triangle in square millimeters.

8. **Estimation** Which is the best estimate of the area of a triangle that has a base of 23.62 cm and a height of 8.33 cm?

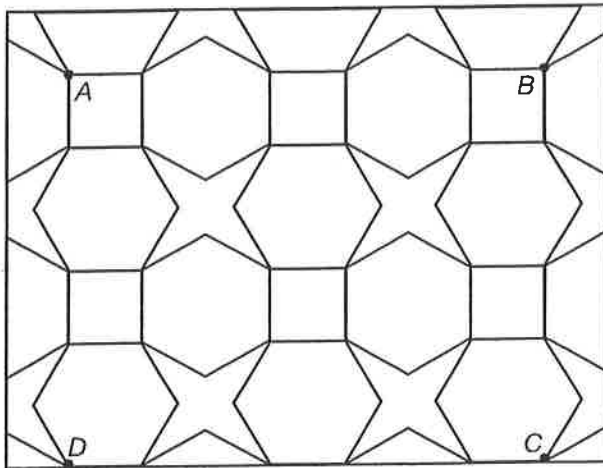
- A 200 cm² B 160 cm² C 100 cm² D 50 cm²

9. **Reasoning** The area of a triangle is 36 cm². Give 3 possible sets of dimensions for the triangle and explain whether or not you can also give the triangles' side lengths.

Name _____

Design Patterns

Reasoning



Three shapes, a square, a hexagon, and an eight-sided star, are repeated in the design. It may not appear so, but the line segments on each polygon are exactly the same length, 1 unit.

1. What is the perimeter of the square, the hexagon, and the star?

2. If the side of the square were doubled, what would happen to its perimeter?

3. If the side of the square were halved, what would happen to its perimeter?

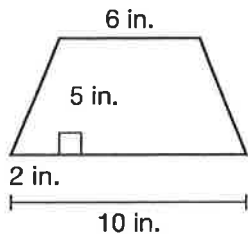
4. If you traced the perimeter of a shape created by joining points *A*, *B*, *C*, and *D*, what would the perimeter be?

5. What fractional part of the perimeter of *ABCD* is formed from the sides of squares that are inside *ABCD*? What is the rest composed of?

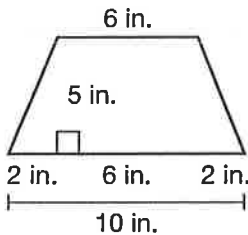
Name _____

Area of Special Quadrilaterals

Find the area of this trapezoid.



Find the area of each part.



Each Triangle

$$A = \frac{1}{2}bh = \frac{1}{2} \times 2 \times 5 = 5 \text{ in}^2$$

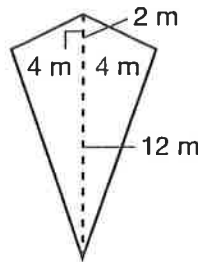
Rectangle

$$A = lw = 6 \times 5 = 30 \text{ in}^2$$

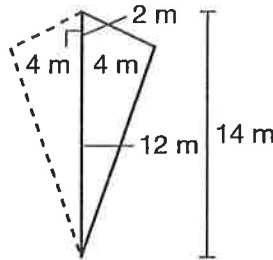
Add the areas together.

$$5 + 5 + 30 = 40 \text{ in}^2$$

Find the area of this kite.



You can find the area of a kite by dividing it into two identical triangles and finding the area of each triangle.

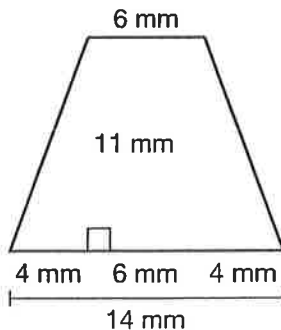


$$A = \frac{1}{2}bh = \frac{1}{2} \times 14 \times 4 = 28$$

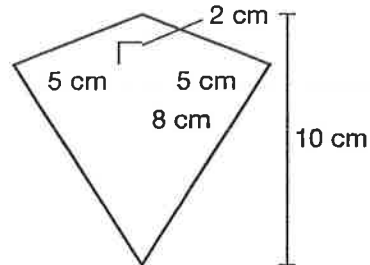
The area of the kite is $2 \times 28 = 56 \text{ m}^2$.

Find the area of the trapezoid or kite.

1.



2.

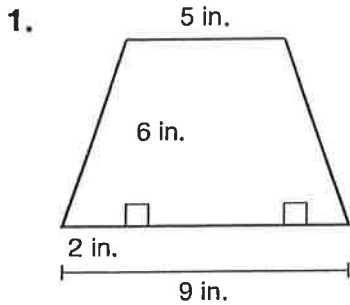


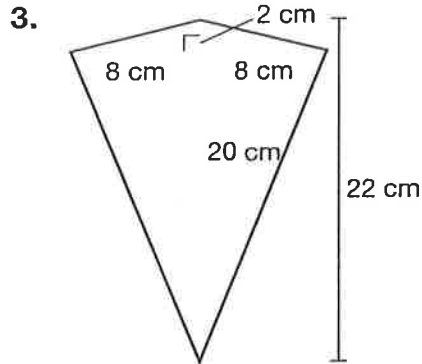
3. Which figure above has a greater area, the trapezoid or the kite? Explain your answer.

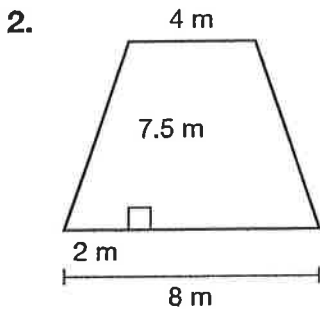
Name _____

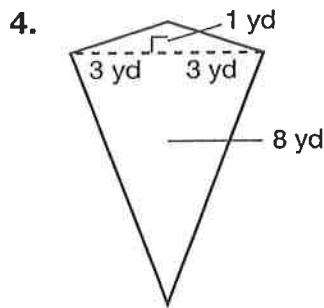
Area of Special Quadrilaterals

Find the area of each figure.



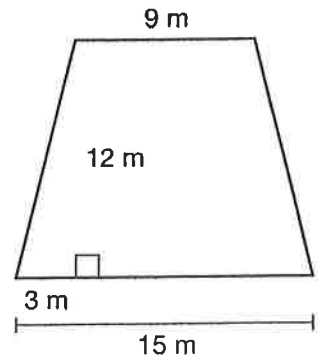




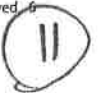
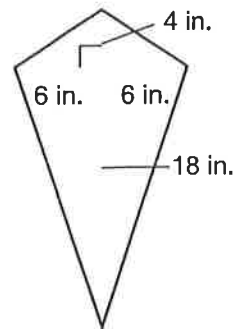


Solve each problem.

5. Rita wants to paint the area shown at the right. What is the area that she needs to cover?



6. **Writing to Explain** Joshua received this kite as a gift. The dimensions were labeled as shown. Joshua says that he does not have enough information to find the area of the kite. Is he correct? Explain your answer.



Name _____

Translations in Space

Visual Thinking



Draw the square $ABCD$.

Draw the diagonal BD .

Redraw the two triangles together to form a parallelogram $EFGH$ where $BD = EH$ and $BC = GH$.

Put the triangles together to form one triangle, IJK , where $BD = IJ$.

Distance $AB = 3$ units.

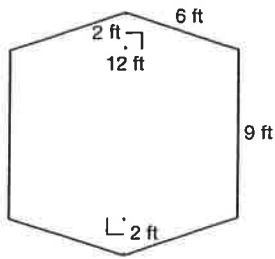
1. What is the area of the square, the parallelogram, triangle IJK , and triangle ABD ?

2. If $AB = 4$ units, what is the area of the square, the parallelogram, triangle IJK , and triangle ABD ?

3. If $AB = n$ units, what happens to the area of triangle ABD or BCD ?

Finding Areas of Polygons

Find the area of this polygon.



Find the area of each part.

Each Triangle:

$$A = \frac{1}{2}bh = \frac{1}{2} \times 12 \times 2 = 12 \text{ ft}^2$$

Rectangle:

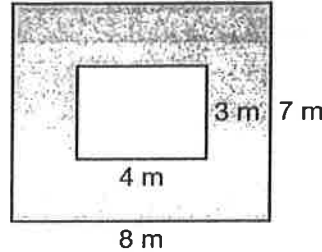
$$A = \ell w = 9 \times 12 = 108 \text{ ft}^2$$

Add the areas together.

$$12 + 12 + 108 = 132 \text{ ft}^2$$

The area of the polygon is 132 ft².

A path around a garden measures 8 m by 7 m. The garden measures 4 m by 3 m. What is the area of the path?



Find the area of the path and the garden together. Then subtract the area of the garden.

Path and garden together:

$$A = \ell w$$

$$A = 8 \times 7$$

$$A = 56 \text{ m}^2$$

Garden:

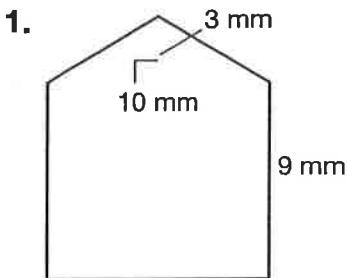
$$A = \ell w$$

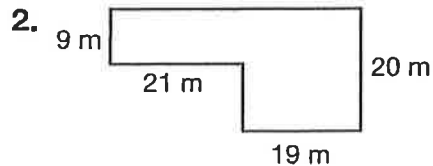
$$A = 4 \times 3$$

$$A = 12 \text{ m}^2$$

$$56 - 12 = 44, \text{ so the area of the path is } 44 \text{ m}^2.$$

Find the area of each figure.



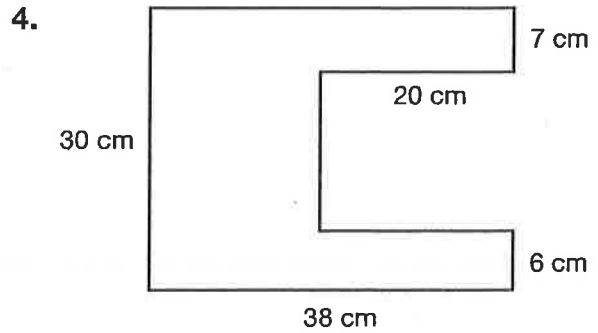
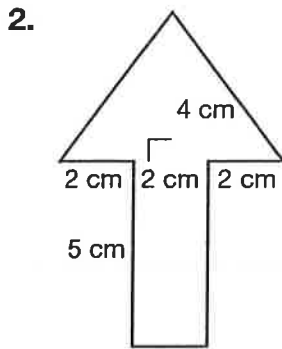
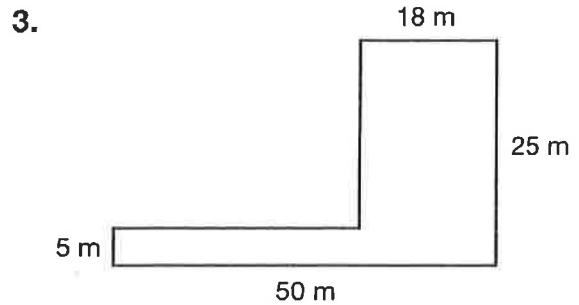
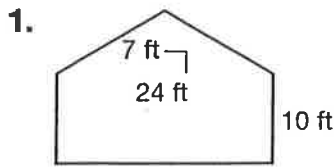


3. The outside of a rectangular path around a rectangular garden measures 4 meters by 7 meters. The garden measures 3 meters by 6 meters. What is the area of the path?

Name _____

Finding Areas of Polygons

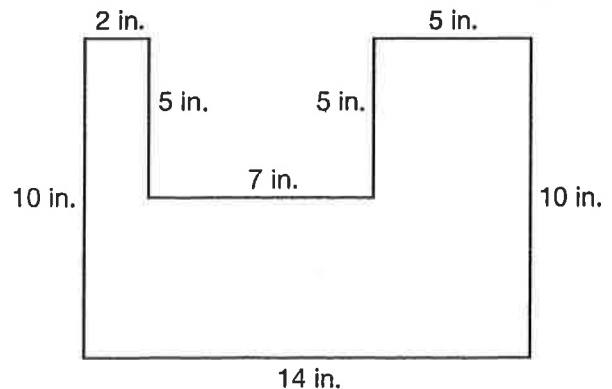
Find the area of each figure.



Read and solve each problem.

5. Carlos is tiling a kitchen counter that is 12 feet by 3 feet. The counter has a rectangular hole 3 feet by 2 feet cut in it for a sink. What is the area of the kitchen counter that Carlos will tile?

6. **Writing to Explain** Explain into which shapes you could break this polygon in order to find its area. Find the area.



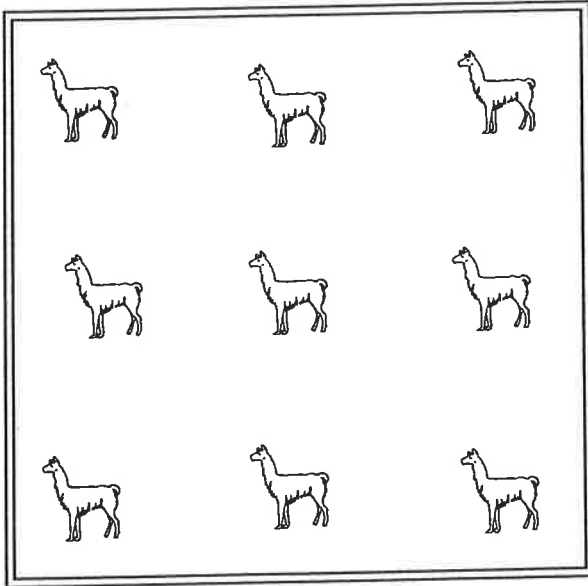
Name _____

Corral the Animals

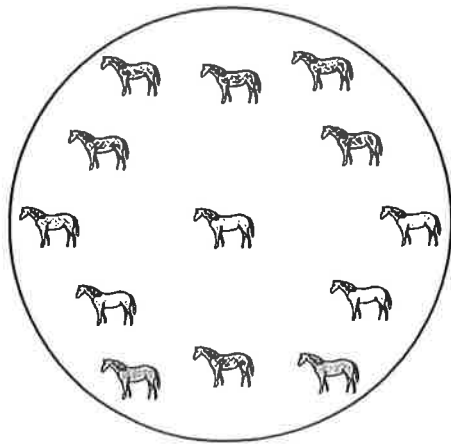
The Granger family raises llamas and horses. They have decided to build new barns to house the animals. They want each animal to have its own space in each barn. Help them by drawing fences on the barn plans below.

Decision Making

1. Draw only 2 square fences on the plan for the square barn so that each of the 9 llamas has its own area.

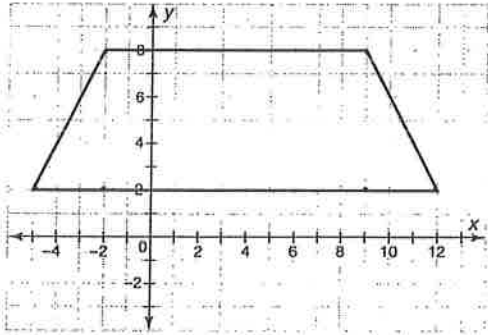


2. Draw only 2 triangular fences on the plan for the circular barn so that each of the 13 horses has its own area.



Areas of Polygons on the Coordinate Plane

To find the area of the polygon on the coordinate grid below, divide the trapezoid into 2 triangles and 1 rectangle. Next, count the squares on the grid or use the absolute value to find the base and height of each triangle and the length and width of the rectangle. Then use these measurements to calculate the area of each part.



Area of each Triangle

$$b = 3, h = 6$$

$$A = \frac{1}{2}bh = \frac{1}{2} \times 3 \times 6 = 9 \text{ sq units}$$

Area of the Rectangle

$$\ell = 11, w = 6$$

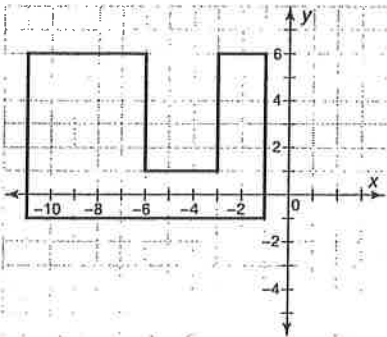
$$A = \ell w = 11 \times 6 = 66 \text{ sq units}$$

Add the areas of the smaller shapes to find the total area of the polygon.

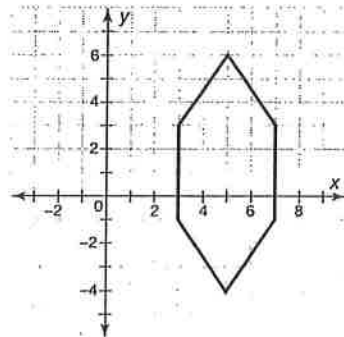
$$9 + 9 + 66 = 84 \text{ square units}$$

Find the area of each polygon.

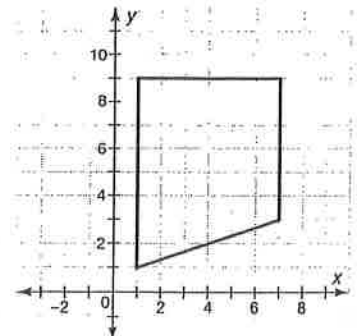
1.



2.

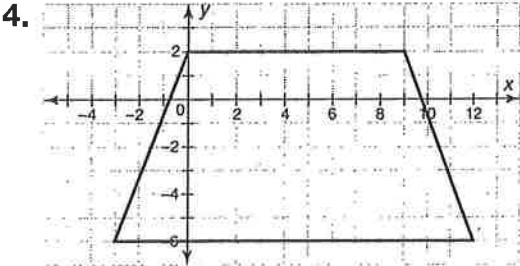
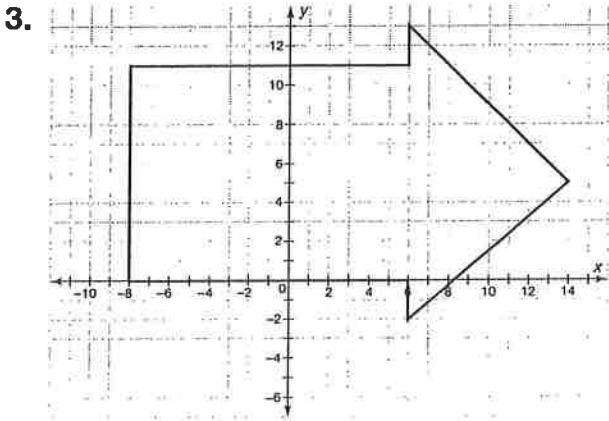
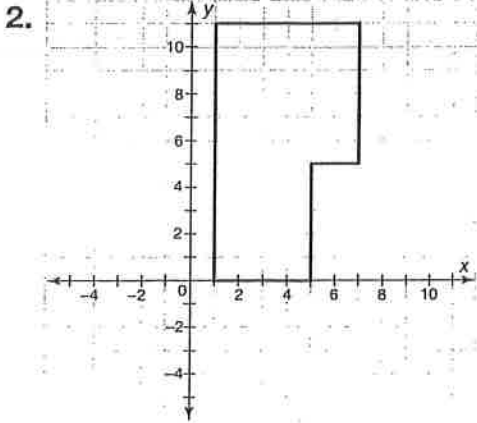
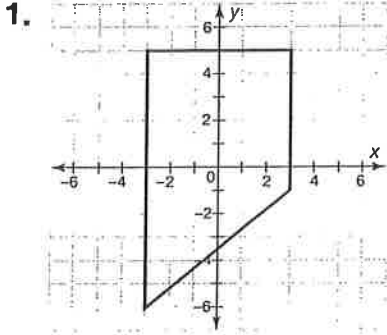


3. **Writing to Explain** Jamal drew a sketch of the garden he is going to plant. Each grid represents 1 sq ft. Each different vegetable will need 3 sq ft, and he wants to plant 12 different vegetables. Does he have enough space in his garden? Explain your answer.



Areas of Polygons on the Coordinate Plane

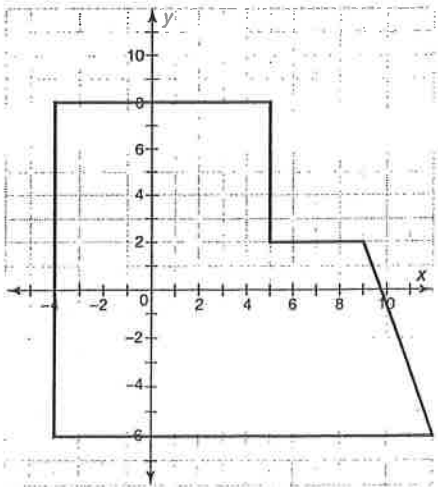
Find the area of each figure.



5. **Reasoning** Which expression can you use to find the area of this figure?

- A $(9 \times 14) + (8 \times 4) + \frac{1}{2}(8 \times 3)$
- B $(8 \times 14) + (9 \times 4) + \frac{1}{2}(9 \times 3)$
- C $(9 \times 14) + (8 \times 4) + (8 \times 3)$
- D $(9 \times 14) + (8 \times 4) + \frac{1}{4}(8 \times 3)$

6. **Model** On a coordinate grid, draw a polygon that has an area of 12 square units. Draw a second polygon that completely encloses the first polygon that has an area of 24 square units.

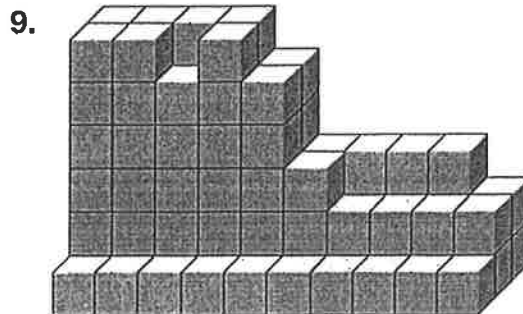
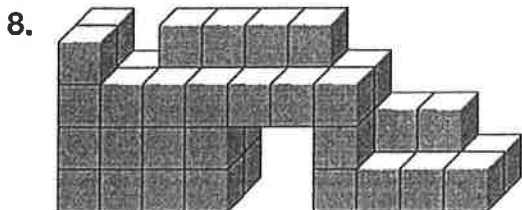
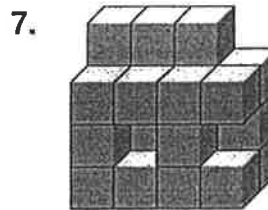
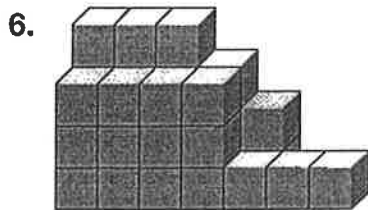
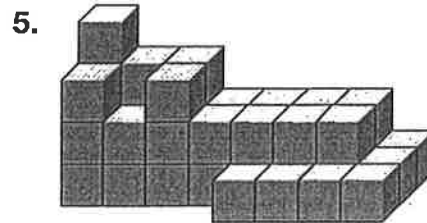
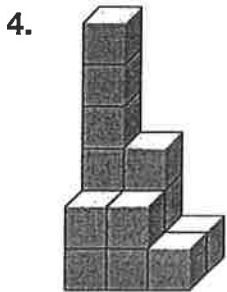
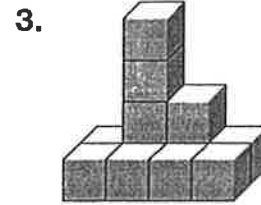
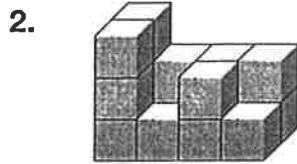
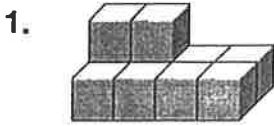


Name _____

On the Blocks

Count the blocks in each structure. Each block sits on top of another, unless the picture shows differently.

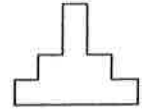
Visual Thinking



Name _____

Problem Solving: Use Objects

Pentomino Construction Company There are 12 different pentominoes. Which two pentominoes can be used to make this shape?



Read and Understand

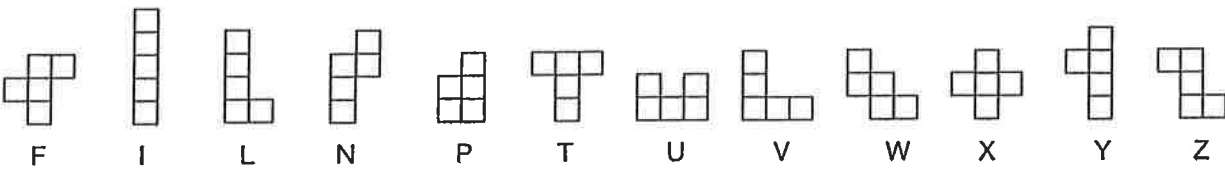
What do you know? There are 12 different pentominoes. Two pentominoes are used to construct this shape.

What are you trying to find? The two pentominoes used to make the shape.

Plan and Solve

What strategy will you use? Use objects, in this case pentominoes.

Study the shape and compare the corners and angles to the group of pentominoes. Choose two pentominoes to make the figure.

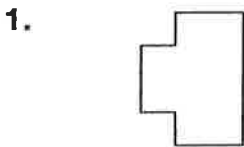


Since the base is 5 units, try the I and the T pentominoes. If your first choice does not work, try other pentominoes.

Look Back and Check

Is your answer reasonable? Yes. The two pentominoes make the same shape.

Fit two pentominoes together to create each shape. Draw the pentominoes used in each figure.

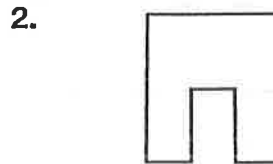
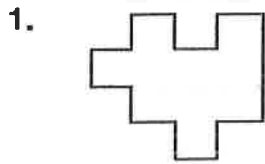


3. **Writing to Explain** A figure is made from three pentominoes. What is the area of the figure in square units? How did you find your answer?

Name _____

Problem Solving: Use Objects

Fit two pentominoes together to create each shape. Draw the pentominoes used in each figure.



3. What is the area in square units of each figure you made in Problems 1 and 2?

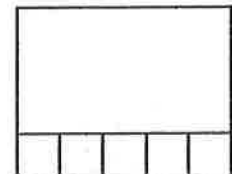
4. Tessa used pentominoes to make this rectangle. The I pentomino is shown. What is the area of the rectangle in square units?

A 5 square units

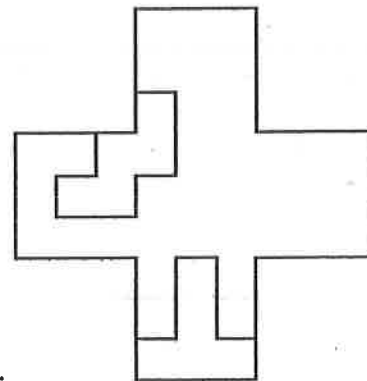
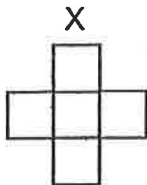
C 20 square units

B 6 square units

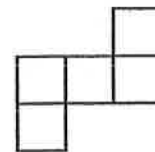
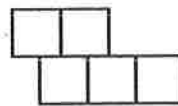
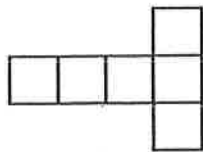
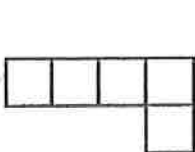
D 25 square units



5. Use nine pentominoes to make a figure that has three times the perimeter of the pentomino X below. Two pentominoes have been placed to get you started.



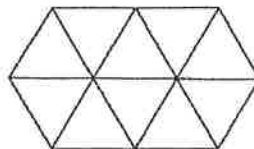
6. **Writing to Explain** Circle the pentominoes. Explain why any figures not circled are not pentominoes.



Name _____

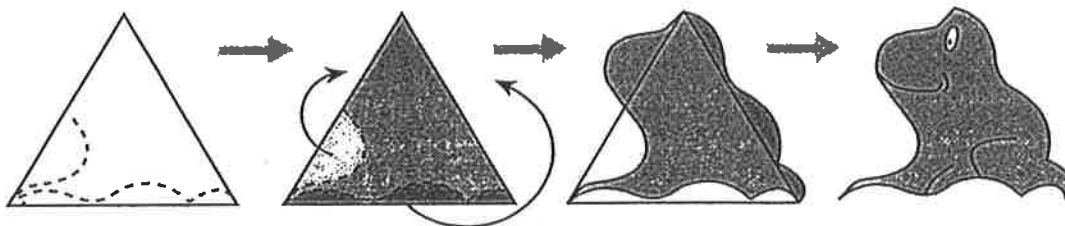
Frog Tiles

Tiles are usually shaped like polygons. For example, the tiles shown at the right are shaped like equilateral triangles.



Visual Thinking

More interesting tiles can be made by changing the shape of a polygon. Notice how a frog-shaped tile can be made by breaking an equilateral triangle into smaller parts and then rearranging those parts.



1. Suppose the triangle that was broken into smaller parts has a base of 3 cm and a height of 2.6 cm. What is the area of the triangle?

2. What is the area of the frog tile? How do you know?

3. What is the total area of a tile pattern made with 10 frog tiles, as shown at the right?

4. Suppose a frog-shaped tile is made from a larger triangle. If the triangle's base is 12 cm and its height is 10.4 cm, what would be the area of a tile pattern made with 50 frog tiles?

